

Package ‘stochcorr’

July 23, 2025

Title Stochastic Correlation Modelling via Circular Diffusion

Version 0.0.1

Description Performs simulation and inference of diffusion processes on circle. Stochastic correlation models based on circular diffusion models are provided. For details see Majumdar, S. and Laha, A.K. (2024) ``Diffusion on the circle and a stochastic correlation model" <[doi:10.48550/arXiv.2412.06343](https://doi.org/10.48550/arXiv.2412.06343)>.

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Suggests ggplot2

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circ.bootstrap	<i>Bootstrap for circdiff</i>
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Description

stoch.bootstrap returns the Bootstrap confidence interval for estimated parameters from circdiff.

Usage

```
circ.bootstrap(est, theta, boot_iter=500, p=0.05, seed = NULL)
```

Arguments

est	object of class cbm or vmp
theta	data of the discretely observed diffusion
boot_iter	number of bootstrap iteration (Default is 500)
p	1-p% confidence interval (Default is 0.05)
seed	(optional) seed value

Details

This function returns a (1-p)% confidence interval for estimated parameters from circdiff using parametric bootstrap. See section 4 of Majumdar and Laha (2024) [doi:10.48550/arXiv.2412.06343](https://doi.org/10.48550/arXiv.2412.06343).

Value

Returns a matrix of the bootstrap (1-p)% confidence interval for the parameters. The first row is the lower bound and the second row is the upper bound.

See Also

[circdiff\(\)](#)

Examples

```

library(stochcorr)

data(wind)

if(requireNamespace("ggplot2")){
  library(ggplot2)
  ggplot2::ggplot(wind, aes(x = Date, y = Dir)) +
    geom_line() +
    labs(title = "Sotavento Wind Farm",
         x = "Date",
         y = "Wind Direction") +
    scale_x_datetime(date_labels = "%d-%b", date_breaks = "2 day") +
    theme_test() +
    theme(
      text = element_text(size = 15),
      axis.text.x = element_text(angle = 90, hjust = 1)
    )
}

a<-circdiff(wind$Dir,10/1440,"vmp")
a

b<-circdiff(wind$Dir,10/1440,"cbm")
b

estimates_vmp<-circ.bootstrap(a,wind$Dir, seed = 100)
estimates_vmp

estimates_cbm<-circ.bootstrap(b,wind$Dir, seed = 100)
estimates_cbm

```

circdiff

Estimation of circular diffusion models

Description

circdiff returns the estimates of parameters of a discretely observed von-Mises process or Circular Brownian motion

Usage

```
circdiff(theta, dt, corr_process, iter=2000, lambda=0, lambda_1=0, lambda_2=0)
```

Arguments

theta	data of the discretely observed diffusion
dt	time step Δt
corr_process	vmp for von-Mises process; cbm for circular brownian motion
iter	number of iterations (Default is 2000)
lambda	regularization parameter for cbm (Default is 0)
lambda_1	regularization parameter for vmp (Default is 0)
lambda_2	regularization parameter for vmp (Default is 0)

Details

Let $\theta_0, \theta_{\Delta t}, \theta_{2\Delta t}, \dots, \theta_{n\Delta t}$ be a discretely observed circular diffusion at time step Δt . The circular diffusion could either be von-Mises process,

$$d\theta_t = -\lambda \sin(\theta_t - \mu)dt + \sigma dW_t$$

or the circular brownian motion,

$$d\theta_t = \sigma dW_t$$

under periodic boundary condition. The function returns the MLE of λ, σ, μ for von-Mises process or σ for circular brownian motion.

We provide an option to perform penalised MLE using an iterative optimization procedure as following, we maximise for von Mises process, where n is the number of observations,

$$\text{Log-lik} - n\lambda_1 \sum (1 - \cos(\theta_{i+1} - \theta_i)) - \lambda_2 \frac{2\lambda}{\sigma^2}$$

For Circular Brownian motion we maximise,

$$\text{Log-lik} - n\lambda \sum (1 - \cos(\theta_{i+1} - \theta_i))$$

See section 3 of Majumdar and Laha (2024) [doi:10.48550/arXiv.2412.06343](https://doi.org/10.48550/arXiv.2412.06343).

Value

A list containing the estimates of the model if corr_process=vmp then it returns

- dt time step Δt
- lambda_vm the drift parameter of the von Mises process
- sigma_vm the volatility parameter of the von Mises process
- mu_vm the mean direction of the von Mises process
- lambda_1, lambda_2 value of the regularization parameters used for estimation

else if corr_process=cbm then it returns

- dt time step Δt
- sigma_cbm the volatility parameter of the circular Brownian motion
- lambda value of the regularization parameter used for estimation

See Also

[circ.bootstrap\(\)](#)

Examples

```
library(stochcorr)

data(wind)
if(requireNamespace("ggplot2")){
  library(ggplot2)
  ggplot2::ggplot(wind, aes(x = Date, y = Dir)) +
    geom_line() +
    labs(title = "Sotavento Wind Farm",
         x = "Date",
         y = "Wind Direction") +
    scale_x_datetime(date_labels = "%d-%b", date_breaks = "2 day") +
    theme_test() +
    theme(
      text = element_text(size = 15),
      axis.text.x = element_text(angle = 90, hjust = 1)
    )
}

a<-circdiff(wind$Dir,10/1440,"vmp")
a

b<-circdiff(wind$Dir,10/1440,"cbm")
b
```

dcbm

Probability transition density function for Circular Brownian Motion

Description

dcbm evaluates the transition density for Circular Brownian Motion

Usage

```
dcbm(theta, t, theta_0, sigma)
```

Arguments

theta	vector of data
t	time step Δt
theta_0	initial value
sigma	sigma

Details

See section 2 of Majumdar and Laha (2024) [doi:10.48550/arXiv.2412.06343](https://doi.org/10.48550/arXiv.2412.06343).

Value

dcbm gives the transition density function of the circular Brownian motion

dvmp	<i>Probability transition density function for von Mises process</i>
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Description

dvmp evaluates the transition density for von Mises process

Usage

```
dvmp(theta, t, theta_0, lambda, sigma, mu)
```

Arguments

theta	vector of data
t	time step Δt
theta_0	initial value
lambda	lambda
sigma	sigma
mu	mu

Details

See section 2 of Majumdar and Laha (2024) [doi:10.48550/arXiv.2412.06343](https://doi.org/10.48550/arXiv.2412.06343).

Value

dvmp gives the transition density function of the von Mises process

ftse2020	2020 USD/GBP and FTSE250 data
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Description

End of the day closing price for USD/GBP and FTSE250 in the year 2020.

Usage

```
data("ftse2020")
```

Format

A data frame with 224 rows and 3 columns:

USD/GBP EOD USD/GBP rate

FTSE250 EOD FTSE250

Date Date

Source

Yahoo Finance

nikkei2020	2020 USD/JPY and Nikkei data
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Description

End of the day closing price for USD/JPY and Nikkei in the year 2020.

Usage

```
data("nikkei2020")
```

Format

A data frame with 213 rows and 3 columns:

USD/JPY EOD USD/JPY rate

Nikkei EOD Nikkei

Date Date

Source

Yahoo Finance

nse2020	2020 USD/INR and NIFTY data
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Description

End of the day closing price for USD/INR and NIFTY in the year 2020.

Usage

```
data("nse2020")
```

Format

A data frame with 250 rows and 3 columns:

USD/INR EOD USD/INR rate

Nifty EOD Nifty

Date Date

Source

Yahoo Finance

rtraj.cbm	Simulate circular Brownian motion
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Description

rtraj.cbm returns a simulated path of a circular Brownian motion for given parameters

Usage

```
rtraj.cbm(n, theta_0, dt, sigma, burnin=1000)
```

Arguments

n	number of steps in the simulated path
theta_0	initial point
dt	Time step
sigma	volatility parameter
burnin	number of initial samples to be rejected (Default is 1000)

Details

Let θ_t evolve according to a circular Brownian motion given by,

$$d\theta_t = \sigma dW_t$$

We simulate θ_t by simulating from its transition density.

Value

A vector of length n of the simulated path from circular Brownian motion

rtraj.vmp	<i>Simulate von Mises process</i>
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Description

rtraj.vmp returns a simulated path of a von Mises process for given parameters

Usage

```
rtraj.vmp(n, theta_0, dt, mu, lambda, sigma)
```

Arguments

n	number of steps in the simulated path
theta_0	initial point
dt	Time step
mu	mean parameter
lambda	drift parameter
sigma	volatility parameter

Details

Let θ_t evolve according to a von Mises process given by,

$$d\theta_t = -\lambda \sin(\theta_t - \mu)dt + \sigma dW_t$$

We simulate θ_t by the Euler-Maruyama discretization of the above SDE.

Value

A vector of length n of the simulated path from von Mises process

stoch.bootstrap	<i>Bootstrap for stochcorr</i>
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Description

stoch.bootstrap returns the Bootstrap confidence interval for estimated rho from stochcorr.

Usage

```
stoch.bootstrap(est, S_1, S_2, boot_iter=500, p=0.05, seed = NULL)
```

Arguments

est	object of class cbm or vmp
S_1	historical price of the first asset
S_2	historical price of the second asset
boot_iter	number of bootstrap iteration (Default is 500)
p	1-p% confidence interval (Default is 0.05)
seed	(optional) seed value

Details

This function returns a p% confidence interval for estimated rho from stochcorr using parametric bootstrap. See section 4 of Majumdar and Laha (2024) [doi:10.48550/arXiv.2412.06343](https://arxiv.org/abs/2412.06343).

Value

Returns a matrix for the bootstrap (1-p)% confidence interval for rho. The first row of the matrix is the lower bound and the second row is the upper bound.

See Also

[stochcorr\(\)](#)

Examples

```
library(stochcorr)

data("nse2020")

## using von Mises process as the correlation process

a <- stochcorr(nse2020$`USD/INR`, nse2020$Nifty, 1 / 250, corr_process = "vmp")
b <- stoch.bootstrap(a, nse2020$`USD/INR`, nse2020$Nifty, seed = 100)

rho_data <- as.data.frame(cbind(a$rho, nse2020$Date))
rho_data[, 2] <- as.Date(rho_data[, 2], origin = "1970-01-01")
```

```

colnames(rho_data) <- c("Correlation", "Time")

if(requireNamespace("ggplot2")){
  library(ggplot2)
  ggplot2::ggplot(rho_data, aes(x = Time, y = Correlation)) +
    theme_test() +
    theme(
      text = element_text(size = 15),
      axis.text.x = element_text(angle = 90, hjust = 1)
    ) +
    geom_line() +
    geom_ribbon(aes(ymin = b[1, ], ymax = b[2, ]), fill = "blue", alpha = 0.15) +
    scale_y_continuous(breaks = round(seq(-1, 1, by = 0.05), 1)) +
    scale_x_date(breaks = "1 month", date_labels = "%B %Y")
}

## using Circular Brownian Motions as the correlation process

a <- stochcorr(nse2020$`USD/INR`, nse2020$Nifty, 1 / 250, corr_process = "cbm")
b <- stoch.bootstrap(a, nse2020$`USD/INR`, nse2020$Nifty, seed = 100)

rho_data <- as.data.frame(cbind(a$rho, nse2020$Date))
rho_data[, 2] <- as.Date(rho_data[, 2], origin = "1970-01-01")
colnames(rho_data) <- c("Correlation", "Time")

if(requireNamespace("ggplot2")){
  library(ggplot2)
  ggplot2::ggplot(rho_data, aes(x = Time, y = Correlation)) +
    theme_test() +
    theme(
      text = element_text(size = 15),
      axis.text.x = element_text(angle = 90, hjust = 1)
    ) +
    geom_line() +
    geom_ribbon(aes(ymin = b[1, ], ymax = b[2, ]), fill = "blue", alpha = 0.15) +
    scale_y_continuous(breaks = round(seq(-1, 1, by = 0.05), 1)) +
    scale_x_date(breaks = "1 month", date_labels = "%B %Y")}

```

stochcorr

Estimate a stochastic correlation model

Description

stochcorr returns the estimates of the instantaneous correlation and other model parameters.

Usage

```
stochcorr(S_1, S_2, dt, corr_process, iter=2000, lambda=4, lambda_1=10, lambda_2=0)
```

Arguments

S_1	Historical price of the first asset
S_2	Historical price of the second asset
dt	Time step
corr_process	specify the correlation process, vmp for von Mises process or cbm for Circular Brownian Motion
iter	Number of iteration (Default is 2000)
lambda	regularization parameter for circular Brownian motion (Default is 4)
lambda_1	(Default is 10)
lambda_2	0 (Default)

Details

Let S_t^1 and S_t^2 be two discretely observed geometric Brownian motions observed at a time step of dt .

$$dS_t^1 = \mu_1 S_t^1 dt + \sigma_1 dW_t^1, dS_t^2 = \mu_2 S_t^2 dt + \sigma_2 (\rho_t dW_t^1 + \sqrt{1 - \rho_t^2} dW_t^2)$$

where $\rho_t = \cos \theta_t$, with θ_t being specified by the von Mises Process ($d\theta_t = \lambda \sin(\theta_t - \mu) + \sigma dW_t^3$) or the Circular Brownian Motion,

$$d\theta = \sigma dW_t^3$$

with periodic boundary conditions. Here W_t^1, W_t^2, W_t^3 are mutually independent Brownian Motions.

We estimate the model by maximising penalized MLE, using an iterative optimization procedure. In case of the von Mises process as the correlation process we maximise,

$$\text{Log-lik} - \lambda_1 \sum (\rho_{i+1} - \rho_i)^2 - \lambda_2 \frac{2\lambda}{\sigma^2}$$

For Circular Brownian motion as the correlation process we maximise,

$$\text{Log-lik} - \lambda \sum (\rho_{i+1} - \rho_i)^2$$

See section 4 of Majumdar and Laha (2024) [doi: 10.48550/arXiv.2412.06343](https://doi.org/10.48550/arXiv.2412.06343).

Value

A list containing the estimates of the model including the asset price parameters, instantaneous correlations and estimates of the correlation process

- rho Estimated instantaneous correlations
- mu_1 Drift of the first asset
- mu_2 Drift of the second asset
- sigma_1 Volatility of the first asset
- sigma_2 Volatility of the second asset

if corr_process=vmp then it additionally returns

- `lambda_vm` the drift parameter of the von Mises process
- `sigma_vm` the volatility parameter of the von Mises process
- `mu_vm` the mean direction of the von Mises process
- `lambda_1`, `lambda_2` value of the regularization parameters used for estimation

else if `corr_process=cbm` then it returns

- `sigma_cbm` the volatility parameter of the circular Brownian motion
- `lambda` value of the regularization parameter used for estimation

See Also

[stoch.bootstrap\(\)](#)

Examples

```
data("nse2020")

## using von Mises process as the correlation process

a <- stochcorr(nse2020$`USD/INR`, nse2020$Nifty, 1 / 250, corr_process = "vmp")

## using Circular Brownian Motions as the correlation process

a <- stochcorr(nse2020$`USD/INR`, nse2020$Nifty, 1 / 250, corr_process = "cbm")
```

stochcorr.sim

Simulate stochastic correlation model

Description

`stochcorr.sim` returns the paths of stock price under a stochastic correlation model

Usage

```
stochcorr.sim(m=500, n, dt, S1_0, S2_0, mu1, sigma1, mu2, sigma2,
mu, lambda, sigma, corr_process)
```

Arguments

<code>m</code>	number of paths (Default is 500)
<code>n</code>	number of steps in each simulated path
<code>dt</code>	time step
<code>S1_0</code>	initial price of the first asset
<code>S2_0</code>	initial price of the second asset
<code>mu1</code>	drift of the first asset

sigma1	volatility of the first asset
mu2	drift of the second asset
sigma2	volatility of the second asset
mu	mean direction of the correlation process (if corr_process=vmp)
lambda	drift of the correlation process (if corr_process=vmp)
sigma	volatility of the correlation process (if corr_process=vmp or corr_process=cbm)
corr_process	specify the correlation process, vmp for von Mises process or cbm for Circular Brownian Motion

Details

This function returns the simulated paths of two stock prices following a stochastic correlation model. See [stochcorr\(\)](#) details of the stochastic correlation model

Value

Returns a list with prices of two assets S1 and S2 under the stochastic correlation model

Examples

```
library(stochcorr)
# Generate 500 paths of two geometric Brownian motions, S1 and S2, of length 100 each
# following the von Mises process with mu=pi/2, lambda=1 and sigma =1

a<-stochcorr.sim(m=500,100,0.01,100,100,0.05,0.05,0.06,0.1,pi/2,1,1,"vmp")
t<-seq(0,100*0.01-0.01,0.01)

# Plot the first realization of S1 and S2

plot(t,a$S1[1,], ylim=c(min(a$S1[1,],a$S2[1,]),max(a$S1[1,],a$S2[1,])),type="l")
lines(t,a$S2[1,], col="red",type="l")
legend(0.01,max(a$S1[1,],a$S2[1,]), legend = c("S1","S2"), col = c("black", "red"), lty=1)
```

s&p2020

2020 EUR/USD and S&P500 data

Description

End of the day closing price for EUR/USD and S&P500 in the year 2020.

Usage

```
data("s&p2020")
```

Format

A data frame with 224 rows and 3 columns:

EUR/USD EOD EUR/USD rate

S&P500 EOD S&P500

Date Date

Source

Yahoo Finance

wind

Wind direction data

Description

Wind direction data from Sotavento Wind farm from 1 November 2024 to 30 November 2024 at a 10 minute frequency.

Usage

```
data("wind")
```

Format

A data frame with 4320 rows and 2 columns:

Dir Wind Direction data

Date Date

Source

<https://www.sotaventogalicia.com/en/technical-area/real-time-data/historical/>

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